

# Markov-modulated nonhomogeneous Poisson processes for dealing with availability bias in surveys of marine mammal abundance

*Roland Langrock (St Andrews)*

*David Borchers (St Andrews)*

*Hans Skaug (Bergen)*



- 1 Motivation and introduction
- 2 Availability model and its incorporation in distance sampling
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## *Conventional distance sampling*

In short:

- 1.) record sightings of animals within predetermined strips
- 2.) quantify number of animals missed within strips
- 3.) scale corresponding estimate up to the area of interest

Details/assumptions involved in 2.):

- model detection probability  $g(x)$  as a function of perpendicular distance  $x$  to trackline
- crucial assumption:  $g(0) = 1$  (certain detection on the line)
- $g(0) \neq 1 \Rightarrow$  abundance estimates (negatively) biased
- for marine mammals typically  $g(0) \neq 1$  (“availability bias”)

## *Existing methods for dealing with availability bias*

- 1.) correction factors
  - very simplistic, can easily lead to substantially biased abundance estimates
- 2.) mark-recapture distance sampling (Borchers et al., 1998)
  - logistically more challenging
  - may suffer from bias due to unmodelled heterogeneity
  - can't deal with animals who regularly dive longer than they are in view
- 3.) explicitly model availability via Poisson process (Skaug and Schweder, 1999)
  - can give good estimates provided that availability events roughly follow a Poisson process

## *Overview of our approach*

Two main reasons for missing whales in surveys:

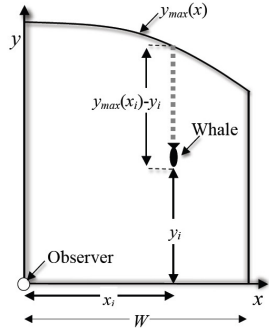
- 1.) animal is underwater
- 2.) animal is at surface but not detected

Our strategy:

- quantify availability via suitable stochastic process
- model conditional detection probability, given the animal is available, as a function of distance from animal to observer
- formulate a corresponding model for detections
- use fitted model to obtain abundance estimates

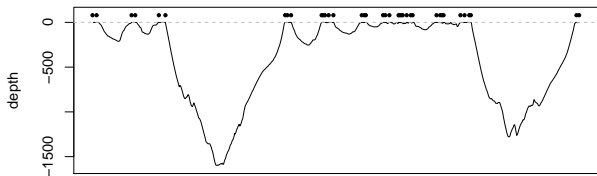
## Model illustration (for a single whale)

- observer at  $(x = 0, y = 0)$
- assume animal movement is negligible  
→ perpendicular distance fixed
- availability events occur according to some stochastic process  
(operating on the forward distance scale)
- detection process = thinned surfacing process  
(thinned according to some detection function)



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## MMPPs for surfacing events



- surfacings are continuous-time events that tend to occur in clusters (due to behavioural switches)
- this motivates the use of Cox processes:
  - Poisson process with rate  $\lambda(I)$
  - $\lambda(I)$ : unobserved non-negative stochastic process
- Markov-modulated Poisson process (MMPP):
  - Cox process where  $\lambda(I)$  is a finite state Markov process
  - extends the approach of Skaug and Schweder (1999)



## Embedding an MMPP in a DS survey

- MMPP can be used to describe surfacings
- but not all surfacings are associated with a detection...
- assume prob. of detections of surfacings to depend on  $x$  and  $y$
- e.g., hazard probability:

$$h(x, y) = \mu \exp\left(-\frac{x^\gamma + y^\gamma}{\sigma^\gamma}\right)$$

- corresponds to a thinning of the MMPP
  - detections are then realizations of a *nonhomogeneous* MMPP, with rates  $\lambda_i h(x, y)$ ,  $i = 1, \dots, N$
- given a fitted nonhomogeneous MMPP, standard techniques can be used to obtain abundance estimates

## Likelihood of nonhomogeneous MMPP for detections

- bad news: in general, for nonhomogeneous MMPPs there is no closed-form likelihood expression available
- good news: we found such an expression for MMPPs with *piecewise constant* rates (i.e.,  $h(x, y)$  a step function)
- this can be exploited to approximate, arbitrarily accurately, the likelihood for any given form of  $h(x, y)$   
(by approximating  $h(x, y)$  by a step function, using a high number of intervals)

## Proposition (single animal likelihood)

Assume that  $h$  is piecewise constant on the intervals  $[i_0, i_1), \dots, [i_{p-1}, i_p]$ . Let  $h^{(r)}$  denote the constant value of  $h(l)$  on the  $r$ th interval and let  $\mathbf{\Lambda}^{(r)} = \text{diag}(\lambda_1 \cdot h^{(r)}, \dots, \lambda_N \cdot h^{(r)})$ . Then the joint density of detections occurring at distances  $l_1 < l_2 < \dots < l_d$ , with  $i_{R_j} \leq l_j \leq i_{R_j+1}$ , is given by

$$f(l_1, l_2, \dots, l_d) = \pi \prod_{j=1}^d \left( \mathcal{P}(l_{j-1}, l_j) \mathbf{\Lambda}^{(R_j+1)} \right) \mathcal{P}(l_d, y_{\max}) \mathbf{1}^t,$$

where  $l_0 = 0$ ,  $\mathbf{1} \in \mathbb{R}^N$  is a row vector of ones, and

$$\mathcal{P}(l_{j-1}, l_j) = \begin{cases} \exp((\mathbf{Q} - \mathbf{\Lambda}^{(R_j+1)})(l_j - l_{j-1})) & \text{if } l_{j-1} \text{ and } l_j \text{ are} \\ & \text{in the same interval} \\ \exp((\mathbf{Q} - \mathbf{\Lambda}^{(R_{j-1}+1)})(i_{R_{j-1}+1} - l_{j-1})) \\ \quad \cdot \prod_{r=R_{j-1}+1}^{R_j-1} \exp((\mathbf{Q} - \mathbf{\Lambda}^{(r+1)})(i_{r+1} - i_r)) \\ \quad \cdot \exp((\mathbf{Q} - \mathbf{\Lambda}^{(R_j+1)})(l_j - i_{R_j})) & \text{otherwise.} \end{cases}$$

## *Further remarks on statistical inference*

- Data required:
  - survey data (perp. and forward distances from observer to sighted animals)
  - auxiliary data (e.g., tag data) on availability (otherwise identifiability issues)
- Inference:
  - 1.) estimate parameters of availability process from auxiliary data
  - 2.) fixing those parameters, use survey data to estimate parameters determining the conditional detection probability
  - 3.) based on fitted model, compute effective strip width, abundance estimates, etc.

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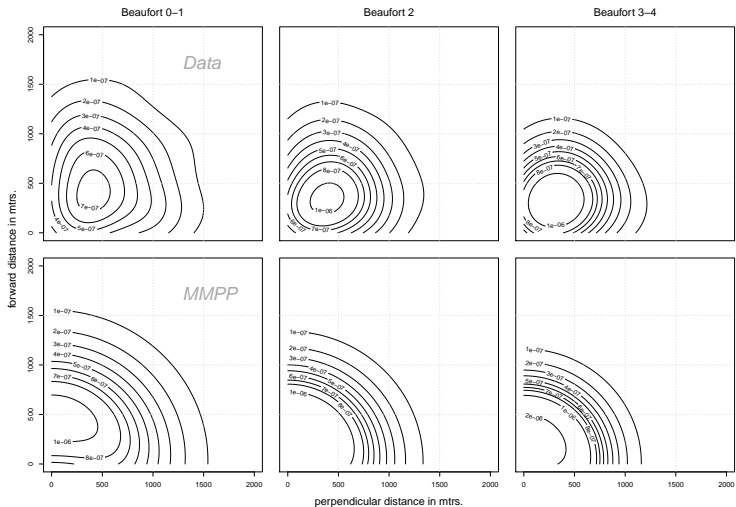
## Minke whale application

- Data:
  - seven sequences of minke whale surfacing events
  - 870 sightings of whales in the Northeastern Atlantic, made during shipboard surveys
- Analysis:
  - MMPPs were fitted to the series of surfacings
  - fixing the MMPP parameters, we estimated the detection probability (given an availability event):

$$h(y, x) = \frac{\theta_1 \theta_2^{\theta_3}}{(\theta_2^2 + x^2 + y^2)^{\theta_3/2}},$$

$$\text{logit}(\theta_2) = \beta_0 + \beta_1 I(B \in \{0, 1\}) + \beta_2 I(B \in \{3, 4\}),$$

with  $B$  giving the sea state in Beaufort (categorical variable)



**Figure:** Bivariate nonparametric density estimates of observed sighting locations (top plots), and bivariate densities of sighting locations predicted by the fitted model (bottom plots).

**Table:** Estimated probability of detecting an animal that is on the trackline,  $g(0)$ , for the three different covariate levels (and 95% confidence intervals obtained through bootstrapping).

	estimate	95% C.I.
$g(0)$ for $B \in \{0, 1\}$	0.75	(0.49,0.80)
$g(0)$ for $B = 2$	0.68	(0.42,0.73)
$g(0)$ for $B \in \{3, 4\}$	0.61	(0.35,0.66)

And minke whales aren't even extreme divers!!

For beaked whales there can easily be a 60% chance of an individual not surfacing at all while within detectable range...







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-  Borchers, D., Zucchini, W., Fewster, R. (1998). Mark-Recapture Models for Line Transect Surveys. *Biometrics*.
-  Skaug, H., Schweder, T. (1999). Hazard Models for Line Transect Surveys with Independent Observers. *Biometrics*.
-  Langrock, R., Borchers, D., Skaug, H. (in press). Markov-modulated nonhomogeneous Poisson processes for modeling detections in surveys of marine mammal abundance. *Journal of the American Statistical Association*.
-  Borchers, D., Zucchini, W., Heide-Jørgensen, M., Cañadas, A., Langrock, R. (in press). Using hidden Markov models to deal with availability bias on line transect surveys. *Biometrics*.

(The slides of this talk can be found on my web page)